M.Sc. Physics Assignment

Classical Mechanics Batch: 2004-2026 The Cochin College

Maximum Marks: 100 Time Allowed: Till 17/1/2025

Instructions:

- 1. Answer all questions.
- 2. All questions carry equal marks.
- 3. Provide detailed solutions and derivations wherever applicable.
- 4. Diagrams must be neat and clearly labeled.
- 1. Calculate the total scattering cross-section for hard-sphere scattering. Show the derivation clearly and discuss the physical implications of the result.
- 2. Calculate the moment of inertia and the principal moments of inertia of a box with masses M placed at each corner. Perform the calculation about an axis passing through one corner of the box along its edge. Clearly define the geometry of the box.
- 3. Discuss the trajectories of a particle moving under a central force field. Derive the relationship between energy and the trajectory. Consider a potential of the form $V(r) = -kr^n$ and explain how n affects the motion.
- 4. Derive the expression for the Coriolis force from first principles. Clearly state the assumptions and conditions under which the Coriolis force is observed.
- 5. A river flows in the northern hemisphere at a latitude of 30° from the equatorial plane. Calculate the Coriolis force acting on the river's flow. Discuss the direction and implications of this force on the river's trajectory.
- 6. Derive the differential equations governing the motion of a rigid body. Use the Euler angles to express the equations and explain their physical significance.
- 7. Differentiate between **Hamilton's Principal Function** and **Hamilton's Characteristic Function**. Provide examples to illustrate their uses in mechanics.
- 8. Draw a diagram of an ellipse representing the Earth-Moon system. Clearly mark the relevant points, including the positions of the Earth and Moon, foci, axes, angles, and the position vector of the Moon. Provide a brief explanation of each feature in the context of orbital mechanics.
- 9. Using the Lagrangian method, derive the relativistic equation of motion for a harmonic oscillator. Discuss the modifications introduced by relativistic effects.
- 10. Starting from the expression for angular momentum, derive the expression for the moment of inertia tensor. Provide a detailed explanation of its components and their significance in the rotational dynamics of rigid bodies.

End of Question Paper